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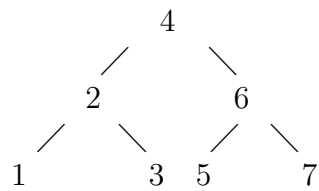
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Data Structure I

SOLVE EXACTLY THREE OUT OF THE FOLLOWING FIVE  
PROBLEMS:

1. a. What is the maximum number of regions defined by  $n$  straight lines in the plane?  
  
b. What is the maximum number of finite regions defined by  $n$  straight lines in the plane?
  
2. Let  $x^{\overline{m}} = x(x+1)\cdots(x+m-1)$   
$$\nabla f(x) = f(x) - f(x-1)$$
what is  $\nabla(x^{\overline{m}})$ ?
  
3. Which of the following statement is true?
  - a. If  $f(N) = O(g(N))$  then  $g(N) = o(f(N))$
  - b. For  $k$  large enough,  $N = O(\log^k N)$
  - c.  $N \log N = O(N^{1+\frac{1}{\log N}})$
  - d. If  $f(N) = O(T(N))$ ,  $g(N) = O(T(N))$  and  $f(N) - g(N) = o(T(N))$  then  $f(N) = O(g(N))$  and  $g(N) = O(f(N))$ .

4. Show the result of inserting 16, 15, 14, 13, 12, 11 to the *AVL* tree



For each insertion, give the resulting tree, indicate you need to do single rotation, double rotation or no rotation.

5. Suppose we have 11 memories with address 0 through 10, if we use the hash function  $h(x) = x \pmod{11}$  and the separate chaining algorithm for storing data, give an example of a data of size 6 that result a chain of length 6.